

## Teaching Plan: B.Sc. (Hons.) Mathematics, Semester-4

### DSC-10: Sequences and Series of Functions

**Weeks 1 to 3:** Pointwise and uniform convergence of sequence of functions, The uniform norm, Cauchy criterion for uniform convergence.

[1]: Chapter 8 (Section 8.1).

**Weeks 4 to 6:** Continuity of the limit function of a sequence of functions, Interchange of the limit and derivative, and the interchange of the limit and integral of a sequence of functions, Bounded convergence theorem.

[1]: Chapter 8 (Section 8.2 up to 8.2.5).

**Weeks 7 and 8:** Pointwise and uniform convergence of series of functions, Theorems on the continuity, and integrability of the sum function of a series of functions.

[1]: Chapter 9 (Section 9.4 [9.4.1 to 9.4.3]).

**Weeks 9 and 10:** Theorem on the differentiability of the sum function of a series of functions, Cauchy criterion, and the Weierstrass  $M$ -test for uniform convergence.

[1]: Chapter 9 (Section 9.4 [9.4.4 to 9.4.6]).

**Week 11:** Definition of a power series, Radius of convergence, Absolute convergence (Cauchy-Hadamard theorem).

[1]: Chapter 9 (Section 9.4 [9.4.7 to 9.4.9 followed by the Remark]).

**Week 12:** Differentiation and integration of power series, Abel's theorem.

[2]: Chapter 4 (Section 26).

**Week 13:** Weierstrass's approximation theorem.

[2]: Chapter 4 (Section 27).

**Week 14:** The exponential and logarithmic functions: Definitions and their basic properties.

[1]: Chapter 8 (Section 8.3).

**Week 15:** The trigonometric functions: Definitions and their basic properties.

[1]: Chapter 8 (Section 8.4).

### Essential Readings

1. Bartle, Robert G., & Sherbert, Donald R. (2011). Introduction to Real Analysis (4th ed.). Wiley India Edition. Indian Reprint.
2. Ross, Kenneth A. (2013). Elementary Analysis: The Theory of Calculus (2nd ed.). Undergraduate Texts in Mathematics, Springer. Indian Reprint.

## **DSC-11: Multivariate Calculus**

**Week 1:** Definition and examples of function of two variables, Level curves and surfaces, Limits and continuity of functions of two variables. [1]: Chapter 11 (Sections 11.1 [up to Example 3], and 11.2).

**Week 2:** Partial differentiation and partial derivatives as slope and rate, Higher order partial derivatives. [1]: Chapter 11 (Section 11.3).

**Week 3:** Tangent planes, Total differential, Differentiability, Chain rule for one independent variable. [1]: Chapter 11 (Sections 11.4 [except Examples 2, and 3], and 11.5 [up to Example 5]).

**Weeks 4 and 5:** Extensions of the chain rule to two independent parameters, Directional derivatives and the gradient, Maximal and normal property of the gradient, Tangent planes and normal lines. [1]: Chapter 11 (Sections 11.5 [Examples 6 to 8], and 11.6).

**Week 6:** Extrema of functions of two variables, Lagrange multipliers method for optimization problems with one constraint. [1]: Chapter 11 (Sections 11.7 [up to Example 6], and 11.8 [Examples 1 and 2]).

**Week 7:** Double integration over rectangular regions. [1]: Chapter 12 (Section 12.1).

**Week 8:** Double integration over nonrectangular regions, Double integrals in polar coordinates. [1]: Chapter 12 (Sections 12.2, and 12.3).

**Week 9:** Triple integral over a parallelepiped, Triple integral over solid regions, Volume by triple integrals. [1]: Chapter 12 (Section 12.5).

**Week 10:** Triple integration in cylindrical and spherical coordinates. [1]: Chapter 12 (Section 12.7).

**Week 11:** Jacobians: Change of variables in double and triple integrals. [1]: Chapter 12 (Section 12.8).

**Week 12:** Vector field, Divergence and curl, Line integrals and its properties, Applications of line integrals to mass and work. [1]: Chapter 13 (Sections 13.1, and 13.2).

**Week 13:** Fundamental theorem for line integrals, Conservative vector fields and path independence, Green's theorem for simply connected region, Area as a line integral. [1]: Chapter 13 (Sections 13.3, and 13.4 [up to Example 3]).

**Weeks 14 and 15:** Surface integrals, Statements of Stokes' theorem and Gauss divergence theorem. [1]: Chapter 13 (Sections 13.5, 13.6, and 13.7 [up to Example 3, for all three respective sections]).

### **Essential Reading**

1. Strauss, Monty J., Bradley, Gerald L., & Smith, Karl J. (2007). Calculus (3rd ed.). Dorling Kindersley (India) Pvt. Ltd. Pearson Education. Indian Reprint.

### **Suggestive Reading**

- Marsden, J. E., Tromba, A., & Weinstein, A. (2004). Basic Multivariable Calculus. Springer (SIE). Indian Reprint.

**Note. 1.** For weeks 9 to 11, please refer to sections **12.4, 12.5, and 12.6** while using the Indian print version.  
**2.** To improve the problem-solving ability, for similar kind of examples based upon the above contents, the Suggestive Reading may be consulted.

## **DSC-12: Numerical Analysis**

**Weeks 1 and 2:** Rate and order of convergence; Bisection method, False position method and their convergence analysis.

[1]: Chapter 1 (Section 1.2).

[1]: Chapter 2 (Sections 2.1, and 2.2).

**Weeks 3 and 4:** Fixed point iteration method, Newton's method, and Secant method, their order of convergence and convergence analysis.

[1]: Chapter 2 (Sections 2.3, 2.4, and 2.5).

**Weeks 5 and 6:** LU decomposition and its application to solve system of linear equations; Iterative methods: Gauss–Jacobi, and Gauss–Seidel methods to solve system of linear equations.

[1]: Chapter 3 (Sections 3.5 [up to Example 3.14], and 3.8 [up to Example 3.23]).

**Weeks 7 to 9:** Lagrange interpolation: Linear and higher order interpolation, and error in it. Divided difference and Newton interpolation, Piecewise linear interpolation.

[1] Chapter 5 (Sections 5.1, 5.3, and 5.5).

**Weeks 10 and 11:** First and higher order approximation for the first derivative and error in the approximation, Second order forward, Backward and central difference approximations for the second derivative.

[1]: Chapter 6 (Section 6.2).

**Weeks 12 and 13:** Numerical integration by closed Newton–Cotes formulae: Trapezoidal rule, Simpson's rule, and its error analysis.

[1]: Chapter 6 (Section 6.4).

**Weeks 14 and 15:** Euler's method to solve ODE's, Modified Euler method, Runge–Kutta Method (fourth-order).

[1]: Chapter 7 (Sections 7.2 [up to Example 7.7], and 7.4 [up to Example 7.14]).

### **Essential Reading**

1. Bradie, Brian. (2006). A Friendly Introduction to Numerical Analysis. Pearson Education India. Dorling Kindersley (India) Pvt. Ltd. Third impression 2011.

## DSE-2(i): Biomathematics

**Week 1:** Using data to formulate a model, Discrete versus Continuous models, A continuous population growth model.

[1]: Chapter 1 (Sections 1 to 3).

**Week 2:** Long-term behavior and equilibrium states, Analyzing equilibrium states.

[1]: Chapter 1 (Sections 6, and 7).

**Week 3:** The Verhulst model for discrete population growth, Administration of drugs.

[1]: Chapter 1 (Section 8).

[2]: Chapter 1 (Section 1.2).

**Week 4:** Differential equation of Chemical Reactions.

[2]: Chapter 4 (Section 4.4)

**Week 5:** Predator-prey models (Function response: Types I, II and III).

[2]: Chapter 4 (Section 4.5).

**Weeks 6 and 7:** Introduction to infectious disease, The spread of an Epidemic: The SIS Model, Interpreting the parameter  $\beta$ , The long-term evolution of the disease, The SIR and SEIR models of an epidemic. [1] Chapter 2 (Sections 1, and 2).

**Week 8:** Phase plane analysis of epidemic model, Stability of equilibrium points.

[1]: Chapter 2 (Sections 3, and 4).

**Week 9:** Classifying the equilibrium state; Local stability.

[1]: Chapter 2 (Section 6).

[2]: Chapter 5 (Section 5.4).

**Week 10:** Limit cycles, Limit cycle criterion and Poincaré-Bendixson theorem (interpretation only with Example 5.6.1). [2]: Chapter 5 (Section 5.6).

**Week 11:** Bifurcation, Bifurcation of a limit cycle. [2]: Chapter 13 (Sections 13.1, and 13.2).

**Week 12:** Discrete bifurcation and period-doubling, Chaos.

[2]: Chapter 13 (Sections 13.3, and 13.4).

**Week 13:** Stability of limit cycles, Introduction of Poincaré plane.

[2]: Chapter 13 (Sections 13.5, and 13.6)

**Weeks 14 and 15:** Modelling molecular evolution: Matrix models of base substitutions for DNA sequences, Jukes-Cantor and Kimura models; Phylogenetic distances.

[3]: Chapter 4 (Sections 4.4, and 4.5).

### Essential Readings

1. Robeva, Raina S., et al. (2008). An Invitation to Biomathematics. Academic press.
2. Jones, D. S., Plank, M. J., & Sleeman, B. D. (2009). Differential Equations and Mathematical Biology (2nd ed.). CRC Press, Taylor & Francis Group.
3. Allman, Elizabeth S., & Rhodes, John A. (2004). Mathematical Models in Biology: An Introduction. Cambridge University Press.

**Note.** For an introduction to the SEIR model, refer to Chapter 4 (Section 4.1) of the textbook: Ellen Kuhl, Computational Epidemiology, 2021, Springer.  
([https://link.springer.com/chapter/10.1007/978-3-030-82890-5\\_4](https://link.springer.com/chapter/10.1007/978-3-030-82890-5_4))

## **DSE-2(ii): Mathematical Modeling**

**Weeks 1 and 2:** Modeling concepts and examples, Scaling of variables, and approximations of functions.

[1]: Chapter 0 (Sections 0.2, 0.3, 0.5, and 0.6).

**Weeks 3 and 4:** SIR and SEIR models for disease spread: Methodology, Standard and solvable SIR models, Basic reproduction number.

[1]: Chapter 7 (Section 7.4.3), and Chapter 8.

**Week 5:** Dieting model with analysis and approximate solutions.

[1]: Chapter 9.

**Weeks 6 and 7:** Stability and the phase plane, Almost linear systems.

[2]: Chapter 6 (Sections 6.1, and 6.2)

**Weeks 8 and 9:** Ecological models: Predators and competitors, Critical points, Oscillating populations, Survival of single species, Peaceful coexistence of two species, Interaction of logistic populations, Wildlife conservation preserve.

[2]: Chapter 6 (Section 6.3).

**Week 10:** Nonlinear mechanical systems: Hard and soft spring oscillations, Damped nonlinear vibrations.

[2]: Chapter 6 (Section 6.4 up to Example 2).

**Weeks 11 and 12:** Monte Carlo simulating deterministic, and probabilistic behavior, Generating random numbers.

[3]: Chapter 5 (Sections 5.1, 5.2, and 5.3).

**Weeks 13 and 14:** Linear programming model: Geometric and algebraic solutions, Simplex method and its tableau format.

[3]: Chapter 7 (Sections 7.2, 7.3, and 7.4).

**Week 15:** Sensitivity analysis.

[3]: Chapter 7 (Section 7.5).

### **Essential Readings**

1. Mickens, Ronald E. (2022). *Mathematical Modelling with Differential Equations*. CRC Press, Taylor & Francis Group.
2. Edwards, C. Henry, Penney, David E., & Calvis, David T. (2023). *Differential Equations and Boundary Value Problems: Computing and Modeling* (6th ed.). Pearson.
3. Giordano, Frank R., Fox, William P., & Horton, Steven B. (2014). *A First Course in Mathematical Modeling* (5th ed.). Brooks/Cole, Cengage Learning India Pvt. Ltd.

**Note.** In the practical syllabus, please refer to 3(ii) [3] Chapter 7 (Projects 7.4 and 7.5).

## **DSE-2(iii): Mechanics**

**Week 1:** Fundamental laws of Newtonian mechanics, Law of parallelogram of forces; Equilibrium of a particle, Lamy's theorem.

[1]: Chapter 1 (Section 1.4).

[1]: Chapter 2 (Section 2.2).

**Weeks 2 and 3:** Equilibrium of a system of particles, External and internal forces, Couples, Reduction of a plane force system, Work, Principle of virtual work, Potential energy and conservative field.

[1]: Chapter 2 (Sections 2.3, and 2.4).

**Weeks 4 and 5:** Mass centers, Centers of gravity, Friction.

[1]: Chapter 3 (Sections 3.1, and 3.2).

**Week 6:** Kinematics of a particle, Motion of a particle.

[1]: Chapter 4 (Section 4.1).

[1]: Chapter 5 (Section 5.1).

**Weeks 7 and 8:** Motion of a system, Principle of linear momentum, Motion of mass center, Principle of angular momentum, Motion relative to mass center, Principle of energy, D'Alembert's principle; Moving frames of reference, Frames of reference with uniform translational velocity, Frames of reference with constant angular velocity.

[1]: Chapter 5 (Sections 5.2, and 5.3).

**Weeks 9 and 10:** Applications in plane dynamics- Motion of a projectile, Harmonic oscillators, General motion under central forces.

[1]: Chapter 6 (Sections 6.1 to 6.4).

**Week 11:** Planetary orbits.

[1]: Chapter 6 (Section 6.5).

**Weeks 12 and 13:** Shearing stress, Pressure, Perfect fluid, Pressure at a point in a fluid, Transmissibility of liquid pressure, Compression, Specific gravity.

[2]: Chapter 1.

**Weeks 14 and 15:** Pressure of heavy fluid- Pressure at all points in a horizontal plane, Surface of equal density; Thrust on plane surfaces.

[2]: Chapter 2

### **Essential Readings**

1. Synge, J. L., & Griffith, B. A. (2017). Principles of Mechanics (3rd ed.). McGraw-Hill Education. Indian Reprint.
2. Ramsey, A. S. (2017). Hydrostatics. Cambridge University Press. Indian Reprint.

**Teaching Plan: B.A. (Prog.) with Mathematics as Major,  
and B.Sc. (Physical Sc./Mathematical Sc.), Semester-4**

**DSC-4, and DSE-2(ii): Introduction to Graph Theory**

**Week 1:** Graphs and their representation, Pseudographs, Subgraphs, Degree sequence, Euler's theorem.

[1]: Chapter 9 (Sections 9.1, and 9.2).

**Week 2:** Isomorphism of Graphs, Paths and Circuits, Connected graphs, Eulerian circuits.

[1]: Chapter 9 (Section 9.3).

[1]: Chapter 10 (Section 10.1 [Theorems 10.1.4, and 10.1.5 without proofs]).

**Week 3:** Hamiltonian paths cycles, Adjacency Matrix.

[1]: Chapter 10 (Sections 10.2 [Theorems 10.2.4, and 10.2.6 without proofs, exclude 10.2.3], and 10.3).

**Week 4:** Weighted graphs, Travelling salesman problem, Shortest path problem, Dijkstra's algorithm (without proof), Dijkstra's algorithm improved (without proof).

[1]: Chapter 10 (Section 10.4 up to 10.4.3 [applications only]).

**Week 5:** The Chinese postman problem; Digraphs, Bellman-Ford algorithm.

[1]: Chapter 11 (Sections 11.1, and 11.2).

**Week 6:** Tournaments, Directed network, Scheduling problem.

[1]: Chapter 11 (Sections 11.4, and 11.5).

**Weeks 7 and 8:** Trees and their properties, Spanning Trees.

[1]: Chapter 12 (Sections 12.1 [with exercise 26 on forest], and 12.2 [Theorem 12.2.3 without proof]).

**Week 9 and 10:** Minimum Spanning Tree Algorithms: Kruskal's algorithm, Prim's algorithm (without proofs), Acyclic digraphs and Bellman's algorithm.

[1]: Chapter 12 (Sections 12.3, and 12.4 [Proposition 12.4.5, and corollary 12.4.6 without proofs]).

**Week 11:** Planar graphs, Euler's formula, Kuratowski theorem.

[1]: Chapter 13 (Section 13.1).

**Week 12:** Graph coloring, Applications of graph coloring.

[1]: Chapter 13 (Section 13.2 [Theorem 13.2.4 without proof]).

**Week 13:** Circuit testing and facilities design.

[1]: Chapter 13 (Section 13.3).

**Week 14 and 15:** Flows and cuts, Max flow-min cut theorem, Matchings, Hall's theorem.

[1]: Chapter 14 (Sections 14.1, 14.2, and 14.4).

**Essential Reading**

1. Goodaire, Edgar G., & Parmenter, Michael M. (2011). Discrete Mathematics with Graph Theory (3rd ed.). Pearson Education Pvt. Ltd. Indian Reprint.

**Teaching Plan: B.A. /B.Sc. (Prog.) with Mathematics,  
and B.Sc. (Physical Sc./Mathematical Sc.), Semester-4**

**Discipline A-4: Abstract Algebra**

**Weeks 1 and 2:** Modular arithmetic; Definition and examples of groups, Elementary properties of groups.

[1]: Chapter 0 (up to page 7, and Exercises 3, 7, 9 and 11).

[1]: Chapter 2.

**Weeks 3 and 4:** Order of a group and order of an element of a group; Subgroups and its examples, Subgroup tests; Center of a group and centralizer of an element of a group.

[1]: Chapter 3.

**Week 5:** Cyclic groups and its properties, Generators of a cyclic group.

[1]: Chapter 4 (up to page 80).

**Weeks 6 and 7:** Group of symmetries; Permutation groups, Cyclic decomposition of permutations and its properties, Even and odd permutations and the alternating group.

[1]: Chapter 1.

[1]: Chapter 5 (Examples 1 to 9 and illustrations of Theorems 5.1 to 5.7 without proofs).

**Weeks 8 and 9:** Cosets and Lagrange's theorem; Definition and examples of normal subgroups, Quotient groups.

[1]: Chapter 7 (up to Corollary 5, page 143).

[1]: Chapter 9 (up to Example 11, page 178).

**Week 10:** Group homomorphisms and properties.

[1]: Chapter 10 (up to Example 14, page 202).

**Weeks 11 to 13:** Definition, examples and properties of rings, subrings, integral domains, fields, Characteristic of a ring.

[1]: Chapters 12, and 13.

**Weeks 14 and 15:** Ideals and factor rings; Ring homomorphisms and properties.

[1]: Chapter 14 (up to Example 9, page 251).

[1]: Chapter 15 (Definition and Examples 1 to 7, and properties of ring homomorphisms, up to Corollary 2, page 268).

**Essential Reading**

1. Gallian, Joseph. A. (2017). Contemporary Abstract Algebra (9th ed.). Cengage Learning India Private Limited, Delhi. Indian Reprint (2021).



## Teaching Plan: B.Sc. (Physical Sc./Mathematical Sc.), Semester-4

### DSE-2(i): Elements of Discrete Mathematics

**Week 1:** Sets, Propositions and logical operations.

[2]: Chapter 1 (Section 1.1), and Chapter 2 (Section 2.1).

**Week 2:** Conditional statements, Mathematical induction.

[2]: Chapter 2 (Sections 2.2, and 2.4).

**Week 3:** Relations and equivalence relation, Equivalence classes, Partial order relation, Partially ordered set.

[1]: Chapter 1 (Section 1.1, up to the Definition of POSET).

[2]: Chapter 4 (Sections 4.2 (up to Example 16), 4.4, and 4.5).

**Weeks 4 and 5:** Hasse diagrams, Chain, Maximal and minimal elements, Least and greatest elements, Least upper bound, greatest lower bound in POSETS, Zorn's lemma, Functions and bijective functions.

[1]: Chapter 1 (Sections 1.1 to 1.4).

[2]: Chapter 5 (Section 5.1).

**Week 6 and 7:** Functions between POSETS, Order isomorphism, Lattice as a POSET, Lattice as an algebra and their equivalence.

[1]: Chapter 1 (Sections 1.5 to 1.10, and 1.12 to 1.14).

[2]: Chapter 6 (Section 6.1).

**Week 8:** Bounded lattice, Sublattice, Interval in a lattice.

[1]: Chapter 1 (Sections 1.11, 1.15, and 1.16).

**Week 9:** Products and homomorphism of lattices, Isomorphism of lattices.

[1]: Chapter 1 (Sections 1.17 to 1.20).

**Week 10:** Distributive lattices, Complemented lattice, Partition and pentagonal lattice.

[1]: Chapter 1 (Sections 2.1 to 2.10).

**Weeks 11 and 12:** Boolean algebra, De Morgan's laws, Boolean expressions, Truth tables, Logic diagrams.

[1]: Chapter 1 (Sections 3.1 to 3.6).

[2]: Chapter 6 (Section 6.5).

**Week 13:** Boolean functions, Disjunctive normal forms (as join of meets), Minimal forms of Boolean polynomials.

[1]: Chapter 1 (Sections 4.13, and 4.15 to 4.17).

**Week 14:** Quine Mc-Cluskey method, Karnaugh maps.

[1]: Chapter 1 (Sections 6.1 to 6.5).

[2]: Chapter 6 (Section 6.6).

**Week 15:** Switching circuits, Applications of switching circuits.

[1]: Chapter 2 (Sections 7, and 8).

### References:

1. Rudolf Lidl, & Gunter Pilz (2004). *Applied Abstract Algebra* (2nd ed.). Undergraduate text in Mathematics, Springer (SIE), Indian Reprint.
2. Bernard Kolman, Robert C. Busby, & Sharon Cutler Ross (2009). *Discrete Mathematical Structures* (6th ed.). Pearson education Inc., Indian reprint.

## **DSE-2(iii), and GE-4(ii) (Generic Elective): Linear Programming**

**Weeks 1 and 2:** Standard form of the LPP, graphical method of solution, basic feasible solutions, and convexity.

[1]: Chapter 2 (Section 2.2).

[1]: Chapter 3 (Sections 3.1, 3.2, and 3.9).

**Weeks 3 and 4:** Introduction to the simplex method: Optimality criterion and unboundedness, Simplex tableau and examples.

[1]: Chapter 3 (Sections 3.3, 3.4, and 3.5).

**Weeks 5 and 6:** Artificial variables, Introduction to duality, Formulation of the dual problem with examples.

[1]: Chapter 3 (Section 3.6).

[1]: Chapter 4 (Sections 4.1, 4.2, and 4.3 [Examples 4.3.1, and 4.3.2]).

**Weeks 7 to 9:** Definition of transportation problem, finding initial basic feasible solution using Northwest-corner method, Least-cost method, and Vogel approximation method; Algorithm for solving transportation problems (Only minimization, balanced and non-degenerate transportation problems to be done).

[2]: Chapter 5 (Sections 5.1, and 5.3).

**Weeks 10 and 11:** Hungarian method of solving assignment problem.

[2]: Chapter 5 (Section 5.4).

**Weeks 12 to 15:** Introduction to game theory, rectangular games, Mixed strategies, Dominance principle; Formulation of game to primal and dual linear programming problems.

[1]: Chapter 9 (Sections 9.1, 9.3, 9.4, and 9.6).

[2]: Chapter 15 (Section 15.4).

### **Essential Readings**

1. Thie, Paul R., & Keough, G. E. (2014). *An Introduction to Linear Programming and Game Theory*. (3rd ed.). Wiley India Pvt. Ltd.
2. Taha, Hamdy A. (2017). *Operations Research: An Introduction* (10th ed.). Pearson.

## Teaching Plan for Generic Elective, Semester-4

### GE-4(i): Elements of Real analysis

**Weeks 1 and 2:** Field and order properties of  $\mathbb{R}$ , basic properties and inequalities of the absolute value of a real number.

[1]: Chapter 1 (Sections 1.1, and 1.2).

**Weeks 3 and 4:** Bounded above and bounded below sets, Suprema and infima, The completeness axiom and the Archimedean property of  $\mathbb{R}$ .

[1]: Chapter 1 (Section 1.6 [1.6.1 to 1.6.14, Theorems 1.6.2 and 1.6.10 without proofs]).

[1]: Chapter 1 (Section 1.5 [1.5.1, 1.5.2, and 1.5.9]).

**Weeks 5 and 6:** Convergence of a real sequence, Algebra of limits.

[1]: Chapter 2 (Section 2.1).

[1]: Chapter 2 (Section 2.2 [2.2.1 to 2.2.14, Theorems 2.2.8, 2.2.12, and 2.2.13(d to f) without proofs]).

**Week 7:** The squeeze principle and applications.

[1]: Chapter 2 (Section 2.3 [2.3.1 to 2.3.14, Theorems 2.3.6, 2.3.10, and 2.3.14 without proofs]).

**Weeks 8 and 9:** Monotone sequences, Monotone convergence theorem and applications.

[1]: Chapter 2 (Section 2.5 [2.5.1 to 2.5.10, Theorems 2.5.5 and 2.5.7 without proofs]).

**Week 10:** Cauchy sequences, Cauchy criterion for convergence and applications.

[1]: Chapter 2 (Section 2.7 [2.7.1 to 2.7.6, Theorem 2.7.4 without proof]).

**Week 11:** Convergence and divergence of infinite series of real numbers, Necessary condition for convergence, Cauchy criterion for convergence of series.

[1]: Chapter 2 (Section 8.1).

**Weeks 12 to 14:** Tests for convergence of positive term series, Applications of the integral test, Comparison tests, D'Alembert's ratio test, Cauchy's  $n$ th root test, Raabe's test.

[1]: Chapter 2 (Section 8.2 [8.2.1 to 8.2.12, 8.2.14, 8.2.15, 8.2.17, 8.2.21, and 8.2.22, with all theorems without proofs]).

**Week 15:** Alternating series, Leibniz alternating series test, Absolute and conditional convergence.

[1]: Chapter 2 (Section 8.3 [8.3.1 to 8.3.10, Theorems 8.3.2 and 8.3.4 without proofs]).

### Essential Reading

1. Denlinger, Charles G. (2011). Elements of Real Analysis. Jones & Bartlett India Pvt. Ltd. Student Edition. Reprinted 2015.